

## Number Oddities

The following numbers can be elegantly expressed as symmetrical equations using only the digits of the numbers :

$$369 = (3X69) + (36X9) - (3X6X9) \quad 688 = (6X88) + (68X8) - (6X8X8) \quad 639 = (6X39) + (63X9) - (6X3X9)$$

The following simple equations using three two-digit numbers remain still valid when multiplication signs are introduced between the digits of the numbers. Thus,  $19 + 37 = 56$   $18 + 39 = 57$   $29 + 38 = 67$

and  $(1X9) + (3X7) = (5X6)$   $(1X8) + (3X9) = (5X7)$   $(2X9) + (3X8) = (6X7)$

The simple equation  $13^2 = 169$  is still valid when plus signs are introduced between the digits of 13 and 169,  $(1 + 3)^2 = 1 + 6 + 9$  Here is a curious coincidence,  $2^9 X 9^2 = 2592$

The square number 1089 can be expressed as the difference between the squares of two reversible numbers,  $1089 = 65^2 - 56^2$

Interestingly, it can also be expressed as the difference between two squares in two more ways,  $1089 = 55^2 - 44^2$   $1089 = 183^2 - 190^2$

The numbers 49 and 1680 are unique in that the addition of 1 to them as well to their halves renders them perfect squares. Thus,  $48 + 1 = 49$   $48/2 + 1 = 25$   $1680 + 1 = 1681 = 41^2$   $1680/2 + 1 = 841 = 29^2$

37 is the only two digit number which can be expressed as the difference between the sum of the squares of its digits and the product of its digits,  $37 = (3^2 + 7^2) - 3X7$

The palindromes below can be expressed as the difference between the squares of two reversible numbers,  $2772 = 96^2 - 68^2$   $5445 = 83^2 - 38^2$   $6336 = 80^2 - 08^2$

Below is an interesting oddity involving the square palindrome 69696. This palindrome can be expressed as the product of two palindromes, namely,  $69696 = 6336X11$

The palindrome 6336 is interesting in that it can be represented by a palindromic expression,  $6336 = 8X(63+36)X8$

The square palindromes 121, 12321, 1234321, etc., are interesting. When plus signs are introduced between the digits of these numbers they still remain square, though no longer palindromic. Thus,  $1 + 2 + 1 = 4$   $1 + 2 + 3 + 2 + 1 = 9$   $1 + 2 + 3 + 4 + 3 + 2 + 1 = 16$ .